

What is Claimed is:

1. A method for controlling a physical variable at a frequency of interest ( $f_d$ )

including the steps of:

- a) sampling the physical variable at a sample frequency less than twice the frequency of interest ( $f_d$ );

- b) calculating at least one control command based upon the sampling of the physical variable; and

- c) generating a force for controlling the physical variable based upon the control command.

2. The method of Claim 1, further including the steps of:

- bandpass filtering the physical variable prior to said step a).

3. The method of Claim 2 wherein said bandpass filter extracts a frequency range with a lower bound generally given by  $(2n-1)*f_s/2$  and an upper bound generally given by  $(2n+1)*f_s/2$ , where  $n$  is an integer chosen so that the frequency of interest ( $f_d$ ) is within the extracted frequency range.

4. The method of claim 1 wherein said physical variable includes information within a bandwidth including said frequency of interest and wherein said sampling rate is at least twice the bandwidth of this information.

5. The method of claim 1 further including the step of generating the at least one control command at a rate less than twice the frequency of interest.

6. A method for computing control commands at a reduced rate in a noise or vibration control system including the steps of:

- a) sensing a physical variable;
- b) identifying harmonic components ( $a_k, b_k$ ) of the physical variable at a frequency of interest ( $f_d$ );
- c) down-sampling the harmonic components ( $a_k, b_k$ ) to a lower update frequency ( $f_u$ );
- d) performing control computations on the harmonic components ( $a_k, b_k$ ) at the lower update frequency ( $f_u$ ); and
- e) generating control commands based upon the control computations.

7. The method of Claim 6 further including the step of:

- f) generating harmonic components of the control commands in said step e).

8. The method of Claim 7, further including the step of:

- g) generating a control output at a frequency higher than the lower update frequency.

9. The method of Claim 6 further comprising:

low-pass anti-aliasing filtering to prevent aliasing in sampling at a lower update frequency ( $f_u$ ).

10. The method of Claim 6, further comprising:

obtaining estimates of the harmonic components by computing a fast-Fourier transform of the physical variable; and

extracting the result corresponding to the frequency of interest ( $f_d$ ).

11. The method of Claim 6, wherein said physical variable comprises a plurality of physical variables, said method further including the steps of:

f) generating a sensed signal as a function of each of said plurality of physical variables; and

g) computing harmonic estimates  $z_k$  for each sensed signal  $y_k$  at each sample time  $t_k$  according to  $z_k = z_{k-1} + \rho H(y_k - H^T z_{k-1})$ , where:

$H = [1 \cos(f_d t_k) \sin(f_d t_k) \cos(f_x t_k) \sin(f_x t_k), \dots]^T$  and where:

$f_d t_k$  = desired frequency;

$f_x t_k$  = frequency of unwanted information in  $y_k$ ;

$z_k$  = estimates of harmonic content of  $y_k$  at time  $k$ ;

$z_{k-1}$  = estimates of harmonic content at time  $k-1$ ;

$\rho$  = a variable gain that determines the corner frequency of the first order low-pass anti-aliasing filter;

$y_k$  = sensed signal vector at time k;

$(\cdot)^T$  = transpose of a vector or matrix.

12. The method of Claim 11, further comprising

utilizing every  $N^{\text{th}}$  harmonic estimator output  $z_{Nk}$  where N is the ratio of the sampling frequency and the update frequency ( $f_s/f_u$ ).

13. The method of Claim 11, further comprising:

generating separate control commands for each of multiple tones;

adding control commands for each tone; and

outputting a sum of the control commands for each tone to one or more force

generators.

14. A method for analyzing a physical variable having a first frequency of interest  $f_1$  and a second frequency of interest  $f_2$  including the steps of:

- a) identifying first harmonic components  $a_{k1}$ ,  $b_{k1}$  of the first frequency of interest  $f_1$ ;
- b) down-sampling the harmonic components  $a_{k1}$ ,  $b_{k1}$  at an intermediate frequency  $f_{u1}$ ;
- c) identifying second harmonic components  $a_{k2}$ ,  $b_{k2}$  of a difference between the first frequency of interest  $f_1$  and the second frequency of interest  $f_2$ ;
- d) downsampling the harmonic components  $a_{k2}$ ,  $b_{k2}$  at an update frequency  $f_{u2}$ ; and
- e) analyzing information at the first frequency of interest  $f_1$  and the second frequency of interest  $f_2$  based upon said harmonic components  $a_{k1}$ ,  $b_{k1}$  and  $a_{k2}$ ,  $b_{k2}$ .

15. The method of Claim 14 wherein the intermediate frequency  $f_{u1}$  is higher than the update frequency  $f_{u2}$ .

16. The method of Claim 14 further including the steps of:

- f) generating control signals at the update frequency  $f_{u2}$  based upon said step e).

17. An apparatus for sensing physical variables at a reduced rate comprising:

a sensor adapted to sense physical variables and to generate a sensed signal as a function of the sensed physical variable; and

a control circuit adapted to establish a frequency of interest ( $f_d$ ), and to establish a sample frequency ( $f_s$ ),

wherein the control circuit filters the sensed signals to extract a frequency range with a lower bound given by  $(2n-1)*f_s/2$  and an upper bound given by  $(2n+1)*f_s/2$ , where  $n$  is an integer chosen so that the frequency of interest ( $f_d$ ) is within the extracted frequency range.

18. The apparatus of Claim 17, wherein the control circuit attenuates the filtered sensed signal at a frequency less than the frequency of interest ( $f_d$ ) by high-pass anti-aliasing to produce a resultant signal.

19. The apparatus of Claim 17 wherein the control circuit aliases the filtered sensed signal to a lower frequency when there is no information present at the lower frequency in the sensed signal and the control circuit extracts desired information.